



A new method for deriving ionospheric currents and conductances from Swarm data

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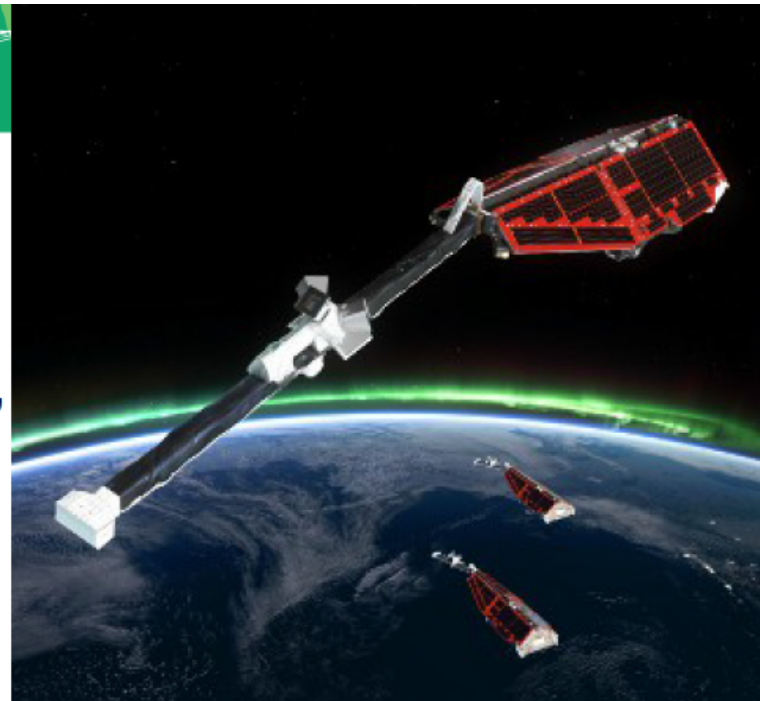
- Swarm satellite mission
- SECS method for Swarm data analysis
- Results from a pilot study with synthetic data
- On Swarm **E**-field calibration and validation
- Prospects for future work



ILMATIETEEN LAITOS
METEOROLOGISKA INSTITUTET
FINNISH METEOROLOGICAL INSTITUTE

Swarm

- Launched 22.11.2013
- 3 identical satellites at low-Earth, near-polar orbits
- Planned mission time 4 years

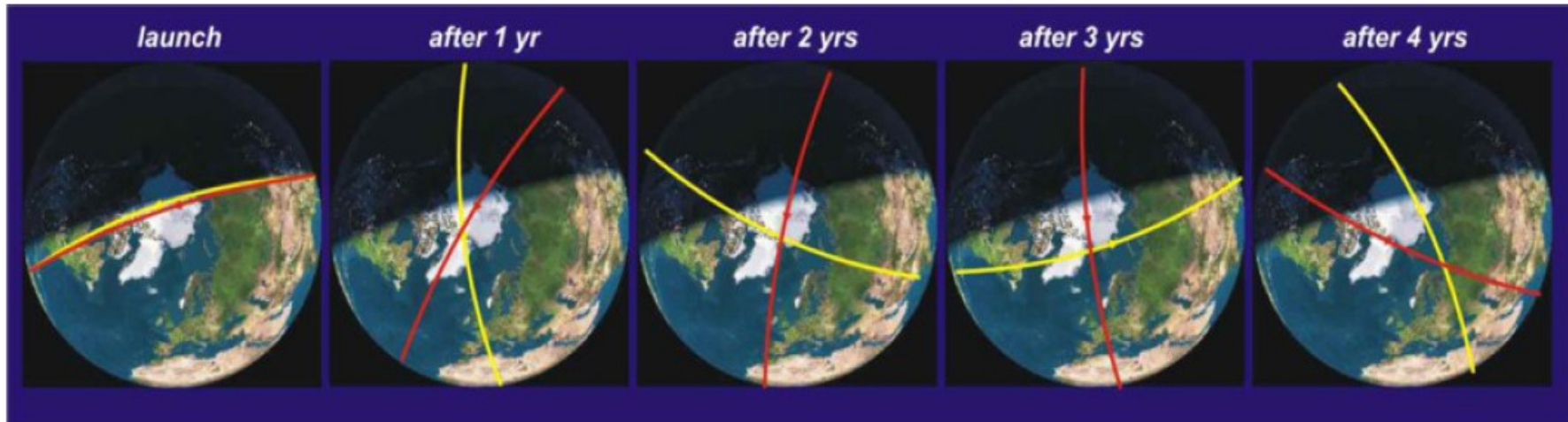


- **Primary objectives:** 1) Geodynamo and core dynamics
2) Lithospheric magnetisation,
3) Electric conductivity of the mantle,
4) **Ionospheric currents**
- **Secondary:** 5) Ocean circulation,
6) Magnetic forcing of the upper atmosphere
- **B , E** , plasma density + temperature, spacecraft acceleration ⁴



Orbits

- **A+C** side-by-side at ~ 450 km, 87.3° inclination, $\sim 1.4^\circ$ separation in longitude, max 10 s difference in equator crossing
- **B** at ~ 510 km, 87.8° inclination



Spherical Elementary Current Systems

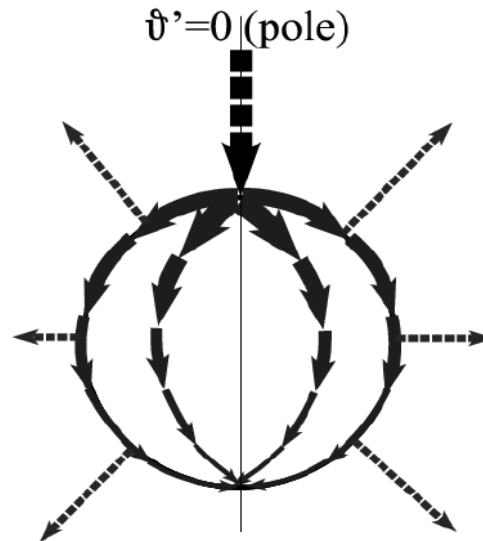
1) Build a grid of SECS
To the area of your
measurements

2) Adjust the intensities
Of SECS so that they fit
to the measurements

Advantage:

The resolution can be
varied according to the
density of observation
points

Jcf

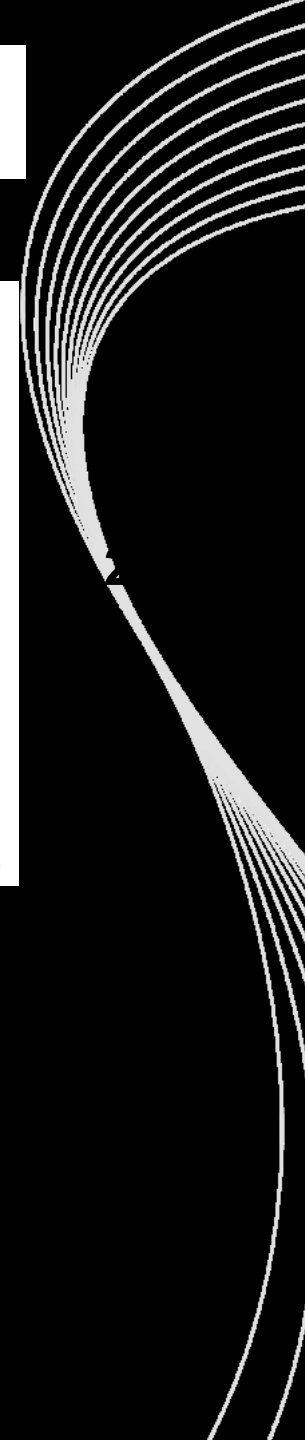
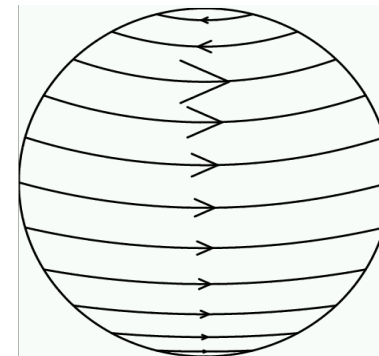
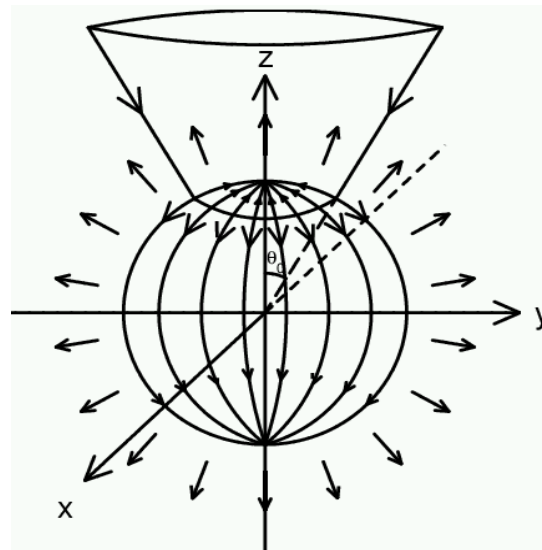


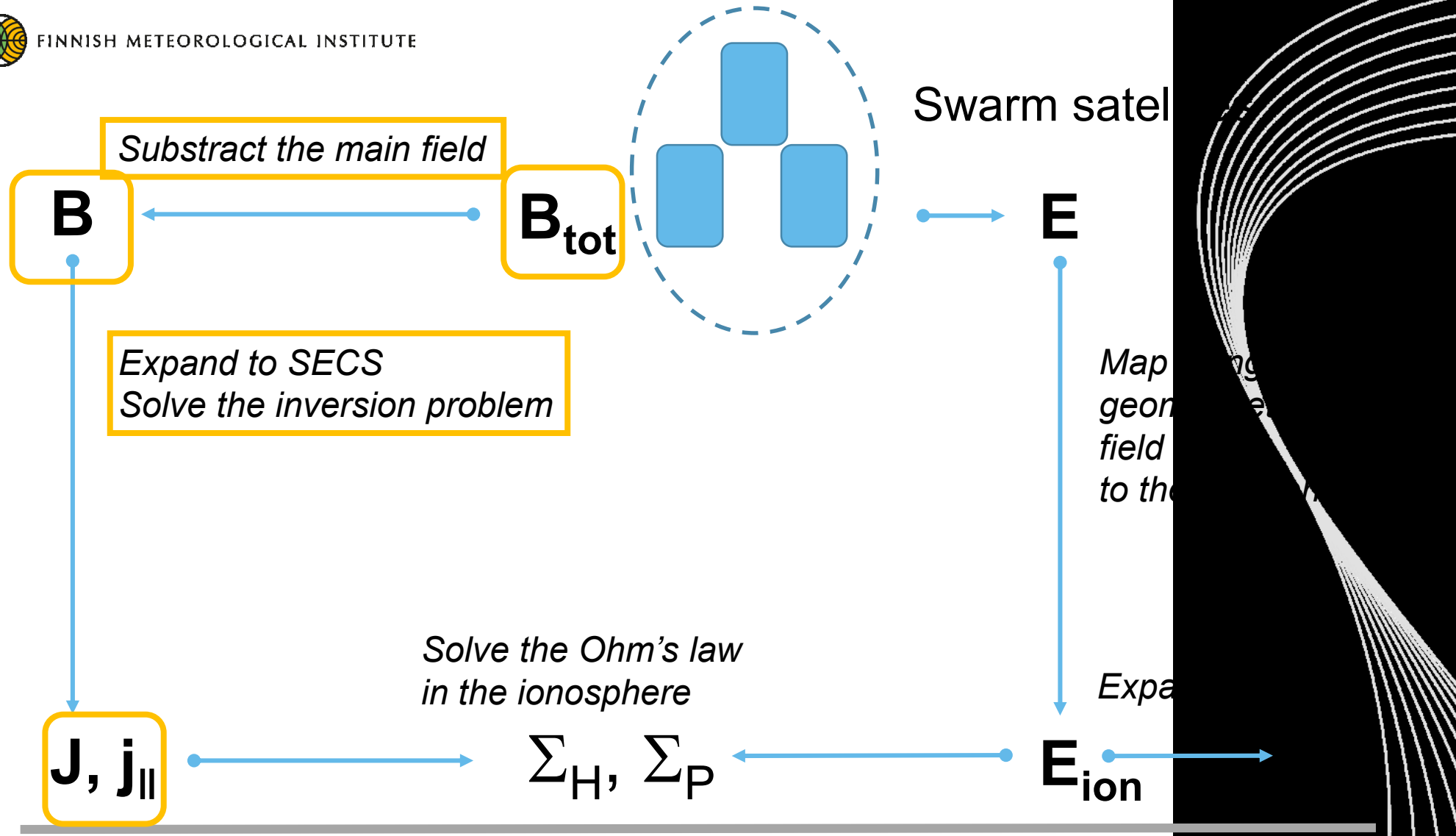
Curl-free elementary system
(with associated FACs)

Jdf



Divergence-free elementary system





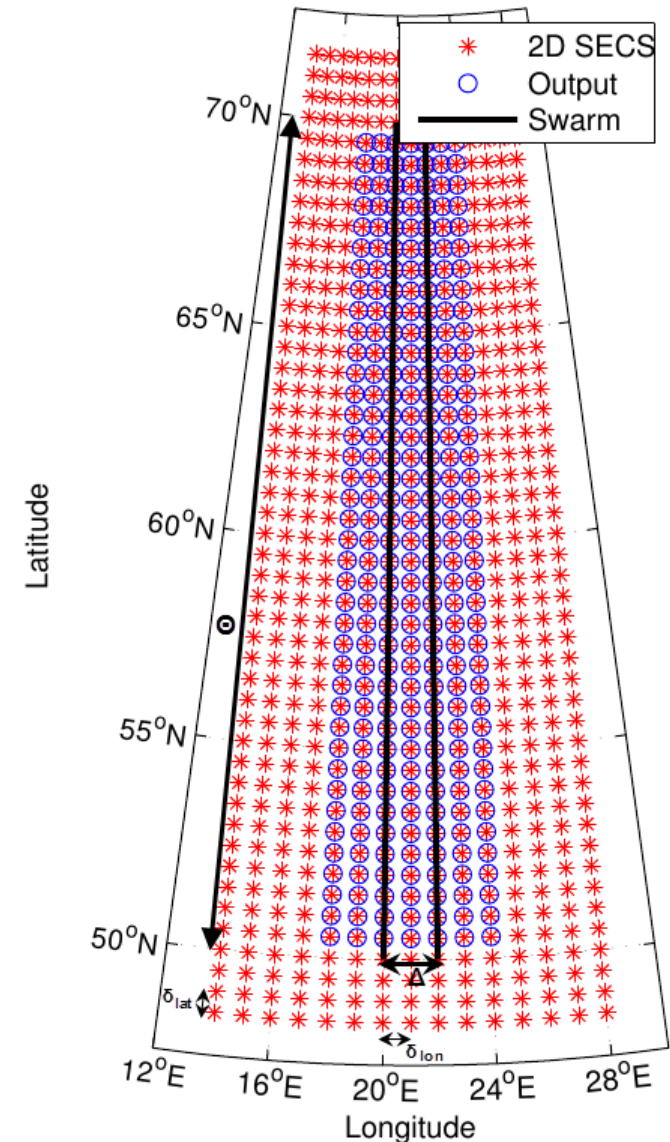
Ionospheric current layer at 110 km altitude



Steps in the analysis

1. Fit 1D div-free systems using only B_r
2. Fit 2D div-free systems using the residual B_r
3. Fit 1D curl-free systems using B_ϕ
4. Fit 2D curl-free systems using the residual B_ϕ and B_θ

1. Fit 1D curl-free systems using only E_θ
2. Fit 2D curl-free systems using the residual E_θ and E_ϕ and





Exploiting synergies between Swarm and Cluster



Three simple test cases:

1. 1D electrojet, no longitudinal variations in E or Σ
2. 2D electrojet, longitudinal variations in E and Σ exists
3. A 2D current vortex

+ Virtual data from MHD simulations

$$RMSError = 100 * \frac{\sqrt{\langle |E_{model} - E_{result}|^2 \rangle}}{\sqrt{\langle |E_{model}|^2 \rangle}}$$

Parameter	Product	Tool
Hall conductance (2D)	▲	▲
Pedersen conductance (2D)	▲	▲
Ionospheric electric field / convection (2D)	▲	▲
Ionospheric horizontal currents (2D)	▲	▲
Field-aligned currents (2D)	▲	▲
Joule heating (2D)	▲	▲
Poynting flux (2D / 3D)	▲	▲

	J_{\perp}	FAC	E	Σ_P	Σ_H
1D Ejet	14.8%	36.0%	4.9%	26.6%	11.6%
2D Ejet	7.9%	42.1%	2.7%	16.1%	12.0%
Vortex	18.7%	155.9%	15.1%	23.0%	22.8%



E-field calibration and validation



The challenge

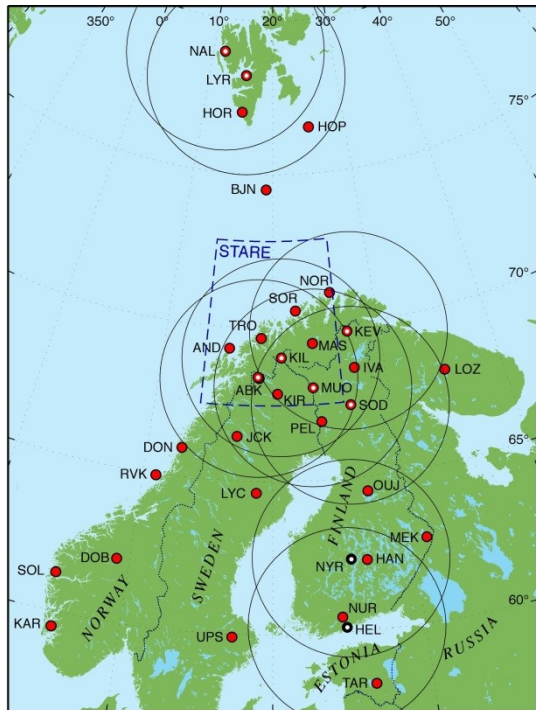
- Swarm **E**-field measured with a new method (High risk – High Gain mission)
- Original plan: Calibration with ground-based radar measurements
- Calibration has appeared to be challenging as error in the signal depends more on the surrounding conditions than anticipated (varies along the orbit)
- Ground-based radar data available only sporadically and typically only one component of **E**
- Can also other ground-based data help in validation? **E**, **B**, and **V** are anyway linked with each other.



Assumption: Swarm-SECS works OK with B

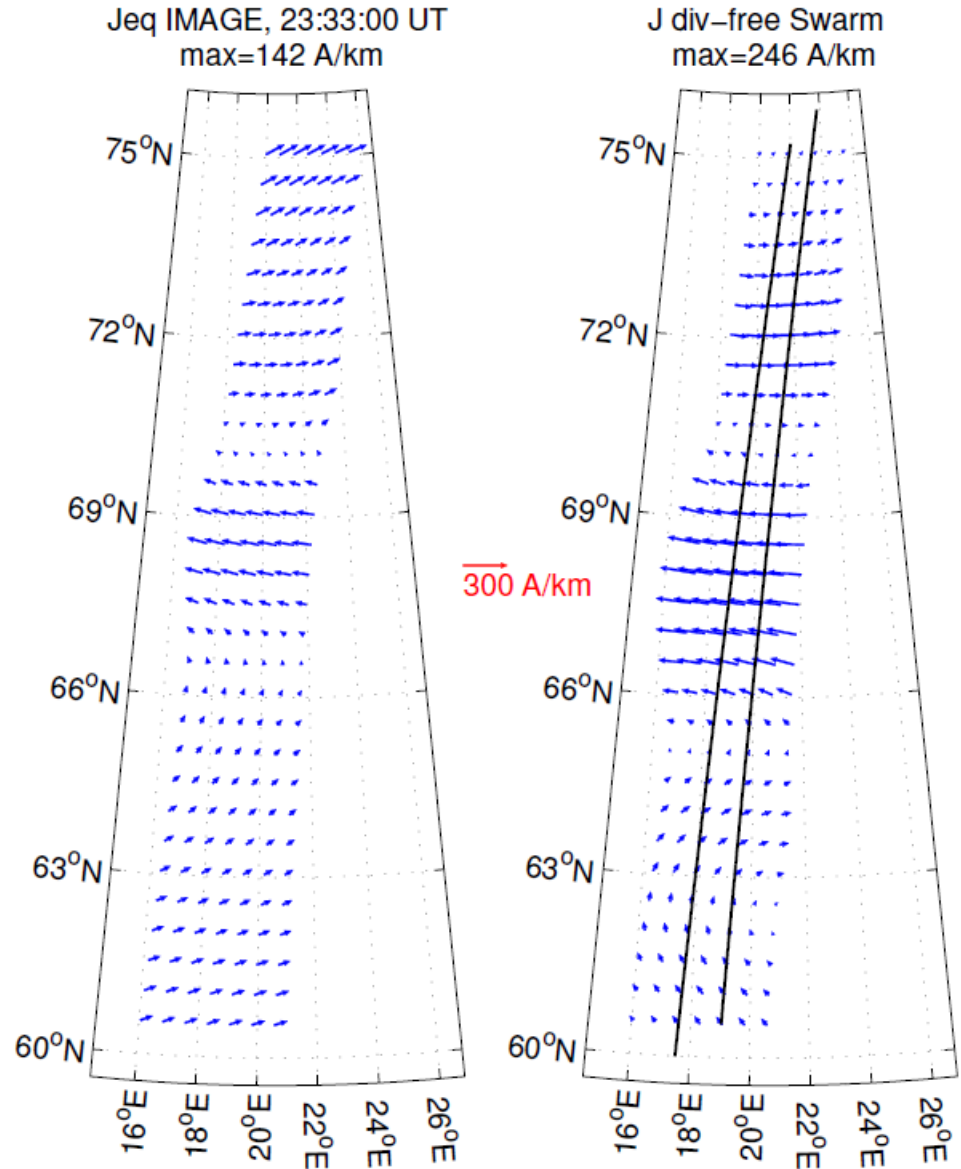
Swarm-SECS J_{df} can be validated with GB magnetometer data

- Potential causes for the differences:
- Baseline selection in IMAGE data
 - Gap in the network at $\sim 72^\circ$



February 2013

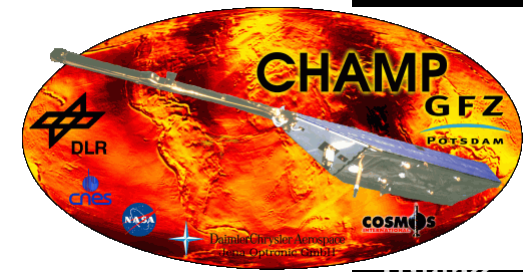
- Magnetometer
- All-sky camera
- Magnetometer and all-sky camera





Assumption: α is typically < 2

- Magnetospheric energy dissipation in the ionosphere
 - Σ_H (Hall conductance) \leftrightarrow auroral precipitation
 - Σ_P (Pedersen conductance) \leftrightarrow Joule heating
- Although Σ_H and Σ_P can themselves vary much, their ratio $\alpha = \Sigma_H / \Sigma_P$ varies typically in the range 0-2.
- Robinson formulas (1987) relate α and Σ_P with electron precipitation energy flux and average energy:
 - $\alpha = 0.45 \langle E \rangle^{0.85}$
 - $\Sigma_P = (40 \langle E \rangle \Psi_E^{0.5}) / (16 + \langle E \rangle^2)$
- For example, $\alpha = 4$ corresponds to $\langle E \rangle > 10$ keV, which is very energetic precipitation (visible in riometer observations, but not necessarily as auroras)



The alpha parameter model

- $\alpha = \Sigma_H / \Sigma_P$, high in the regions where energetic precipitation and thus strong currents in the altitudes around 100 km
- J_ϕ and J_θ derived from CHAMP data (2001-2002, 6112 overflights)
- Use the following formulas:

- Assumptions:

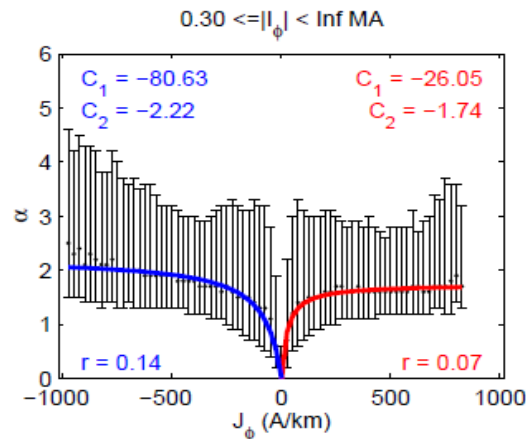
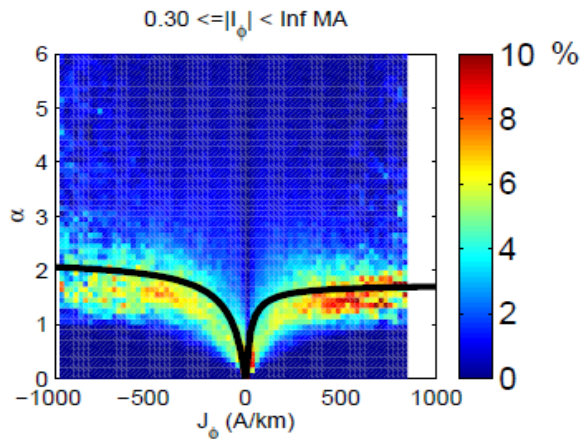
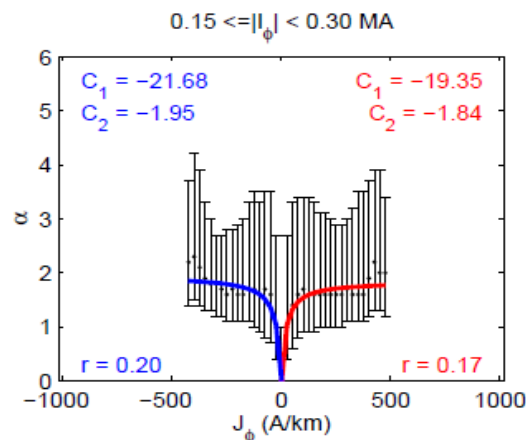
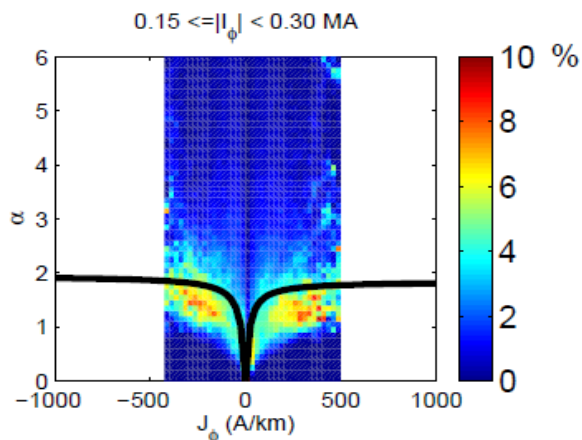
- \mathbf{B} radial, convection \mathbf{E} horizontal
- $E_\phi \ll E_\theta$ (not applicable in the discontinuity region)

$$\mathbf{J} = \Sigma_P \mathbf{E} - \Sigma_H \frac{\mathbf{E} \times \mathbf{B}}{B}$$

$$\mathbf{J} = \underbrace{(\Sigma_P E_\theta + \Sigma_H E_\phi)}_{=J_\theta} \hat{\mathbf{e}}_\theta + \underbrace{(\Sigma_P E_\phi - \Sigma_H E_\theta)}_{=J_\phi} \hat{\mathbf{e}}_\phi.$$

$$\alpha = \frac{\Sigma_H}{\Sigma_P} = \frac{\frac{E_\phi}{E_\theta} + \left(-\frac{J_\phi}{J_\theta}\right)}{1 - \left(-\frac{J_\phi}{J_\theta}\right) \cdot \frac{E_\phi}{E_\theta}},$$

$$\alpha = -\frac{J_\phi}{J_\theta}$$



A statistical fit to χ which can be used with GB magnetometer measuring J_ϕ

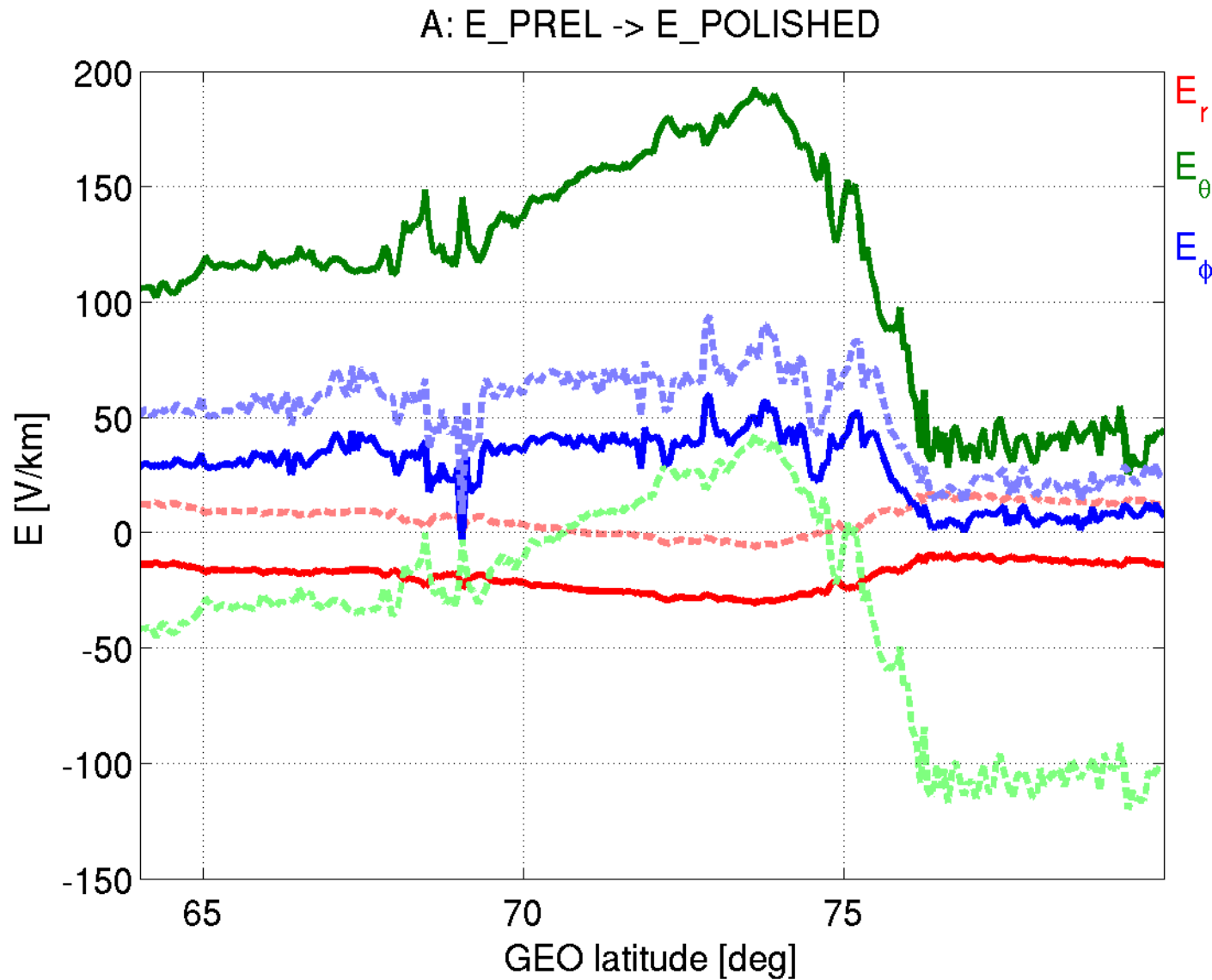
$$\alpha = -\frac{J_\phi}{J_\theta} = \frac{C_2}{\frac{C_1}{|J_\phi|} - 1}$$

Probability of different $\alpha = J_\phi / J_\theta$ as function of J_ϕ

Bin	$C_1 (J_\phi < 0)$	$C_2 (J_\phi < 0)$	$C_1 (J_\phi > 0)$	$C_2 (J_\phi > 0)$
All	-36.54	-2.07	-14.79	-1.73
Quiet	-20.35	-2.19	-46.16	-2.53
Moderate	-21.68	-1.95	-19.35	-1.84
Active	-80.63	-2.22	-26.05	-1.74
Winter	-21.87	-1.99	-13.79	-1.42
Equinox	-49.36	-2.10	-16.55	-1.63
Summer	-18.64	-1.86	-5.88	-1.76



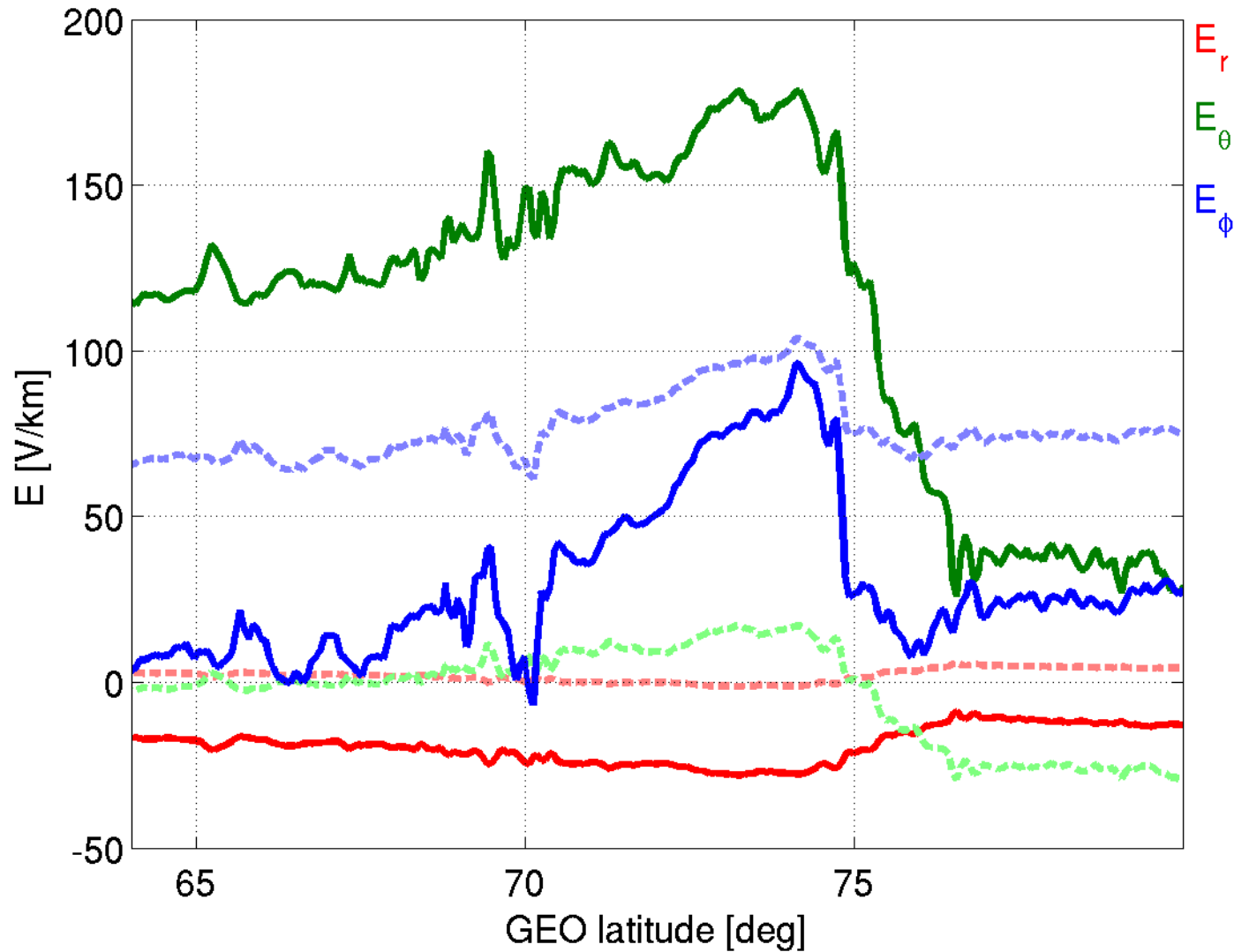
E-field "polishing" Swarm A (Jul 30, 2014, UT 02:10)





E-field "polishing" Swarm C

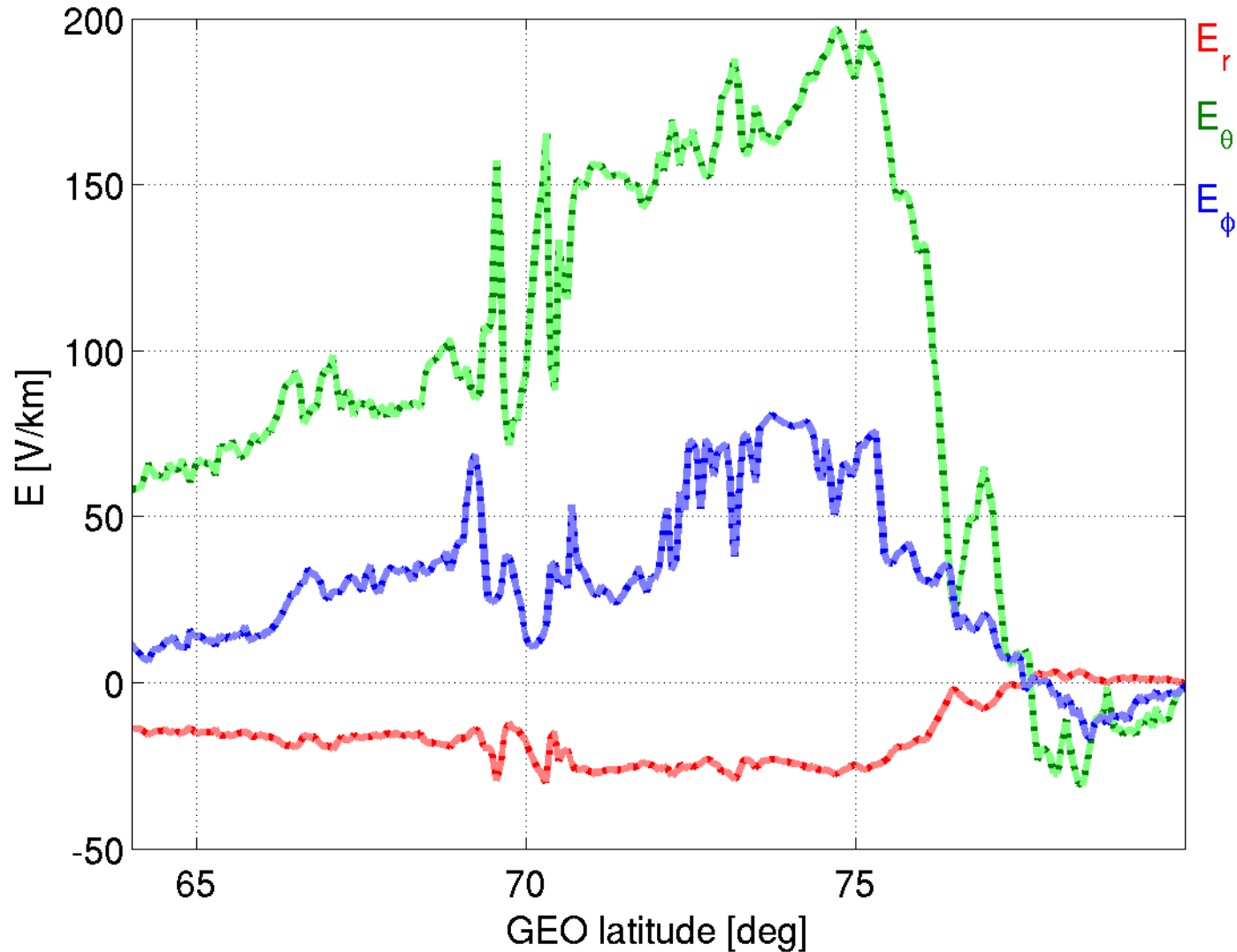
C: E_OPER -> E_POLISHED





E-field "polishing" Swarm B

B: $E_OPER = E_POLISHED$



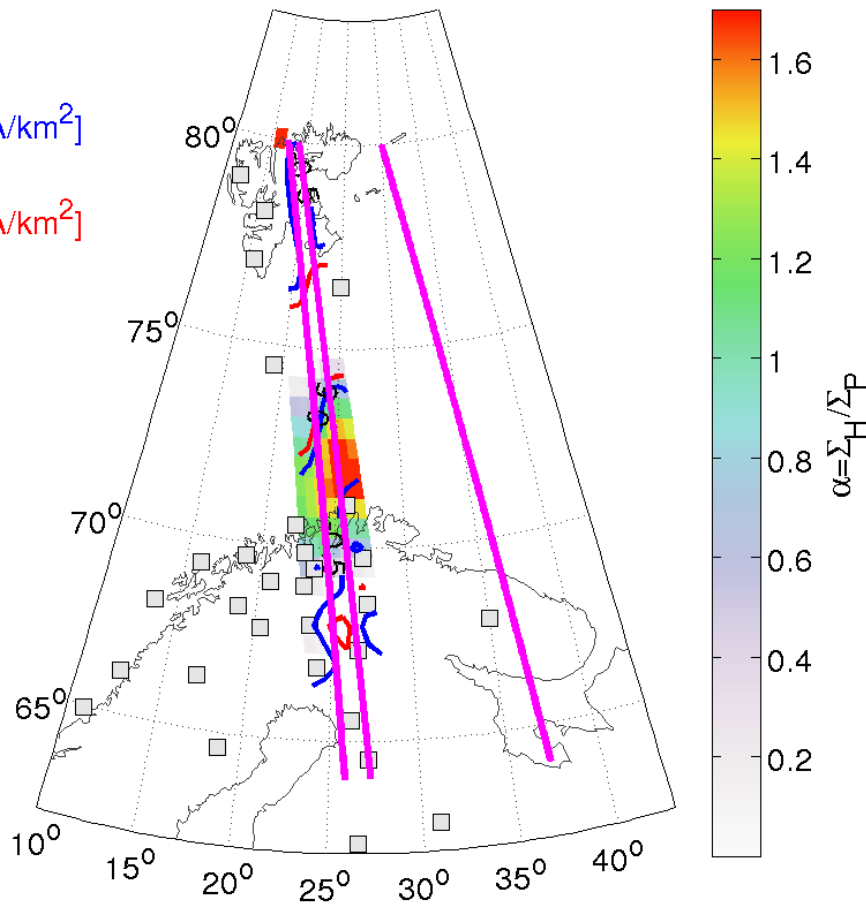


Checking with α -parameter

SECS, **B** and **E**-field

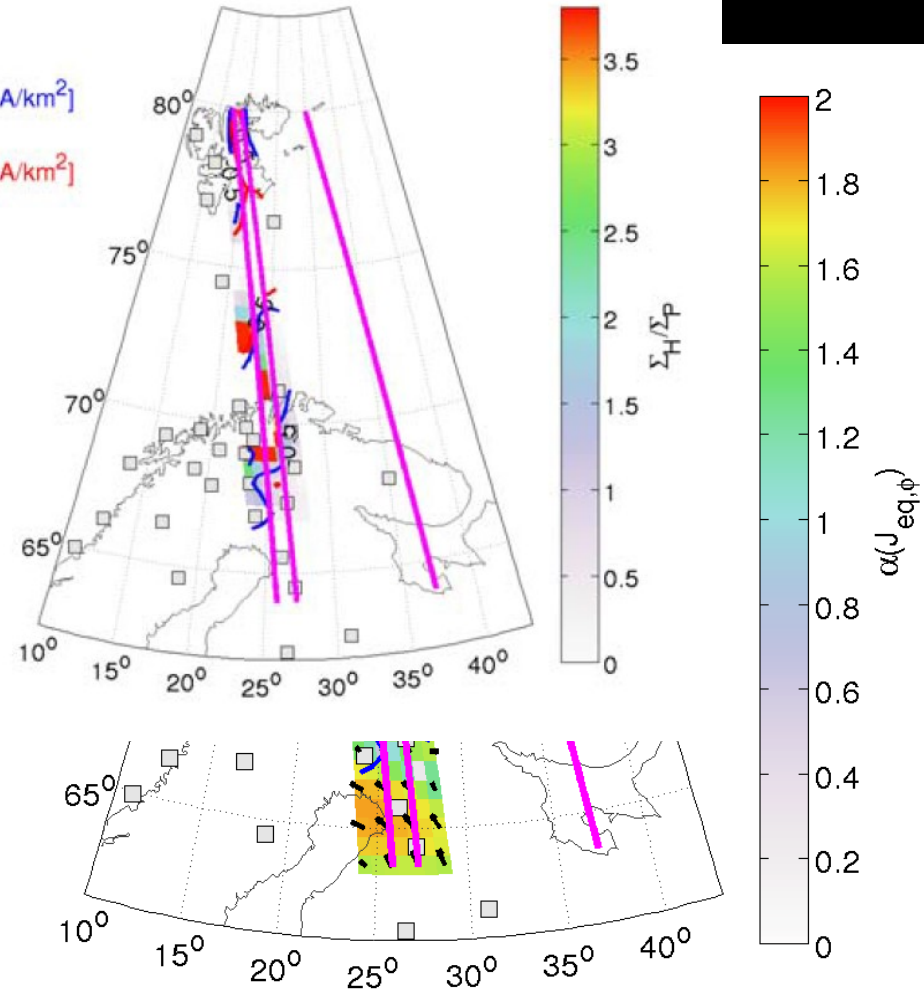
j_{\parallel} [-0.5 A/km²]

j_{\parallel} [0.5 A/km²]



j_{\parallel} [-0.5 A/km²]

j_{\parallel} [0.5 A/km²]





Conclusions and future work

SECS technique for Swarm:

- **Input:** **E** and **B** as input (no support from GB data needed)
- **Output:** 2D strips of
 - **Horizontal currents**
 - **Field aligned currents**
 - **Conductances,**
 - **Electric field,**
 - **Poynting flux**
 - **Joule heating**

Next steps:

- Case studies with GB data (ISR, Themis and MIRACLE), α and **E** observations would help.
- Statistical studies ($J_{df} \leftrightarrow J_{eq}$) to find optimal SECS parameters for massive processing

Tests with Swarm B & E-1000

- Swarm-SECS with **B** works
- In 1D-cases α can be estimated with **B**-data alone
- α can help in **E** quality
- Issues:
 - In our example polished too large
 - The grid used in Swarm seems to have impact on results